# A Physics-Informed Neural Network Approach for Reliable Surrogate Modelling for PWR LOOP Accidents

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## **Background and Motivation**



# Loss-of-offsite Power (LOOP) in PWR

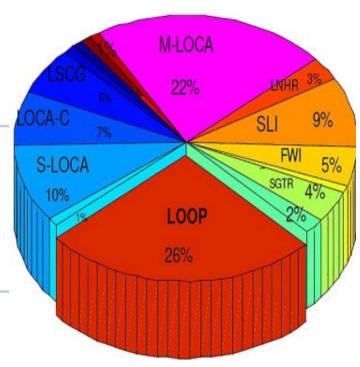


Defined as "The loss of all AC power from the electrical grid to the plant safety buses (NUREG-2122)

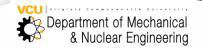
This leads to immediate cessation of the **Primary Coolant Pumps** and the **Main Feedwater Pumps**.

Loss of flow and heat removal capacity triggers rapid temperature and pressure changes.

Contributes 26 % to the core damage frequency (CDF) of Gen II reactors.



**Figure 1.** Initiating events contribution into total CDF of NPP. (Mossoud et at., 2018)



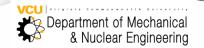
### The Challenge of Real-Time Safety Analysis

LOOP is one of the leading accident reported by NRC in which 33% Switchyard-related events, and 34 % from weather related events between 2009-2023 (Johnson and Ma, 2024).

High-fidelity T/H codes (e.g. MELCOR or RELAP) are too slow for real-time applications (Wang et al., 2024; Antonello et al., 2023).

We need models that is 1000X faster, and provide physically reliable predictions (Zhang et al., 2024; Prantikos et al., 2023).

Develop a surrogate model capable of millisecond predictions of safety-critical parameters ( $T_f$ ,  $P_p$  and  $T_C$ ) during LOOP accidents.



### **Research Objectives and Overview**



### **Surrogate Landscape**



#### Advantages:

- 1. High-speed ML/DNN.
- Less expensive and open source.

#### Challenges:

- 1. Prone to non-conservative errors.
- 2. Physically implausible predictions.
- 3. Remain too slow for real-time Digital Twin application.

#### Gap:

 The need for models that combines speed of data driven models with the physical reliability and consistency.

#### Solution:

 Use of governing physics equations to constrain the neural network's training.



**Develop** a model using physics learning, over purely data learning





**Validate** performance against purely data driven model (DNN) to quantify the benefit of physical constraints

PINN will deliver the needed speed while eliminating the nonconservative errors and ensuring physical consistency

### **Research Approach and Procedure**

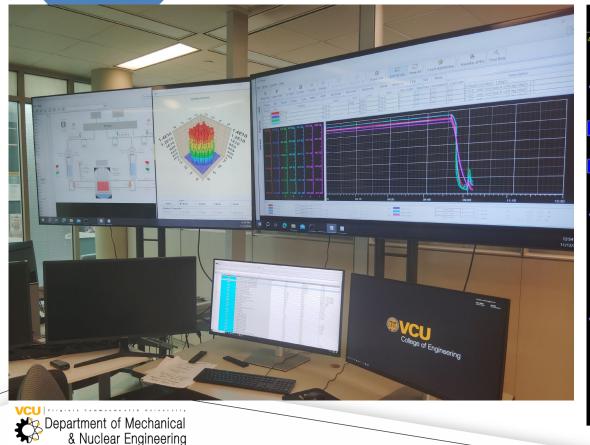


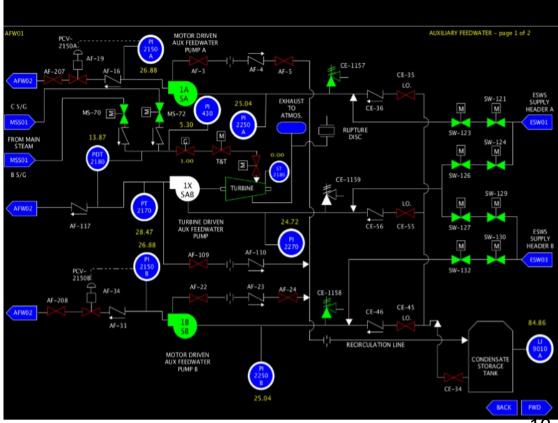
### Research Approach and Procedure

• Running 36 PWR LOOP accidents with Simulator.

Task I

• Each varying in initial condition, and system configuration.





#### **Research Approach and Procedure**



Task II

- Develop 3 Deep Neural Networks (DNN) architectures (Deep-MLP, TCN and ResNet-MLP).
- Training and Validation.

Task III

- Develop 3 Physics-Informed Neural Networks (PINNs) variants (Transfer Learning PINN, ResNet Multi-Head and Neural\_ODE).
- Training and Validation.

Task IV

Model evaluations and comparisons



#### **DNN Surrogate Architectures**

#### **Table 1: DNN Models**

Model	Architecture			
A	MLP (Baseline feed-	Feed-forward benchmark."		
	forward)			
В	Temporal Convolution	Uses <b>convolutional blocks</b> designed to capture the temporal		
	Network (TCN)	dependencies and inertia of the reactor system, making it		
		highly effective for sequence data.		
С	ResNet-MLP hybrid	Leverage residual connections, ensuring training stability.		

#### **Loss Function**

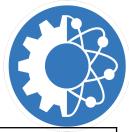
$$L_{total} = \frac{1}{N} \sum_{i=1}^{N} \left[ \left( \dot{T}_{f,i} - T_{f,i} \right)^{2} + \left( \dot{T}_{c,i} - T_{c,i} \right)^{2} + \left( \dot{P}_{p,i} - P_{p,i} \right)^{2} \right]$$

Eq ...1



# **PINN Surrogate Architectures**

#### **Table 2: PINN Models**



Model	Network Architecture	
A	Baseline PINN	A standard fully-connected network constrained by the <b>L_Physics</b> term
В	ResNet Multi-Head	Uses a <b>Shared-Encoder</b> layer, which forces the network to learn a single common latent physical representation of the reactor state.
C	Neural_ODE PINN	Doesn't directly predict, but rather <b>parameterizes the time derivative</b> . The predictions are then generated by running an RK4 (Runge-Kutta)
Department of Mec	harical neering	integrator

### PINN Approach (Physics Loss - "r")



#### **Loss Function**

$$L_{total} = \frac{1}{N} \sum_{i=1}^{N} \left[ \left( \dot{T}_{f,i} - T_{f,i} \right)^2 + \left( \dot{T}_{c,i} - T_{c,i} \right)^2 + \left( \dot{P}_{p,i} - P_{p,i} \right)^2 \right] + \left[ \lambda_{phys} \frac{1}{N} \sum_{i=1}^{N} \left[ r_{1,i}^2 + r_{2,i}^2 + r_{3,i}^2 \right] \right]$$

$$\lambda_{phys} \frac{1}{N} \sum_{i=1}^{N} [r_{1,i}^2 + r_{2,i}^2 + r_{3,i}^2]$$

Eq ...2

#### **Fuel Energy Balance**

$$r_1 = \rho_f c_{p,f} V_f \frac{dT_f}{dt} - Q_{gen}(t) + U_{fc} A_{fc} (T_f - T_c)$$

Eq ...3

#### **Coolant Energy Balance**

$$r_2 = \rho_f c_{p,c} V_c \frac{dT_c}{dt} - U_{fc} A_{fc} \left( T_f - T_c \right) + Q_{AFWS}(t) + Q_{loss}(t)$$

Eq ...4

#### **Simplified Pressure Evolution**

$$r_3 = \frac{dP_p}{dt} - K_p \frac{dT_c}{dt}$$

Eq ...5

### **Results**



### **Speed & Statistical Baseline**

 $\succ$  Both DNN and PINN models achieve prediction time in the millisecond range ( $\sim 10~ms$ )

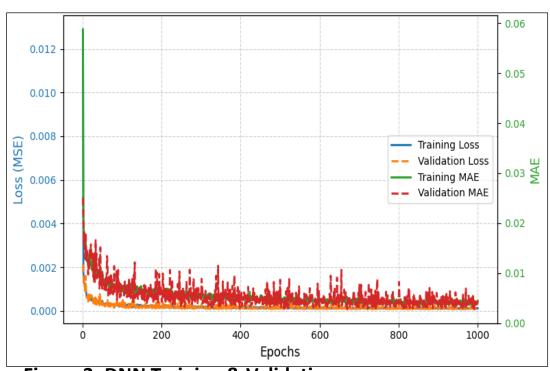


Figure 2: DNN Training & Validation

- $ightharpoonup R^2 \approx$  0.7 (acceptable fit) : NMEA  $\approx$  5.51
- Higher MaxAE and localized losses

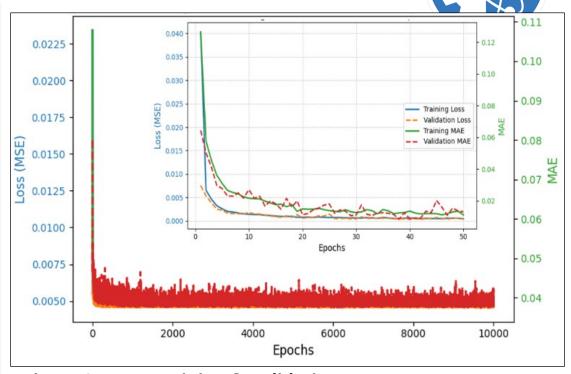
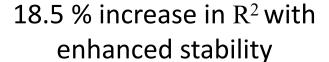
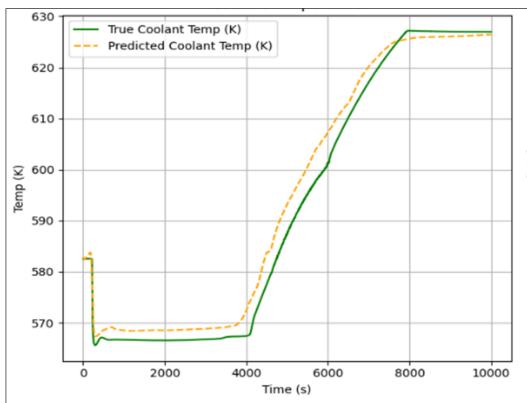


Figure 3: PINN Training & Validation

- $ightharpoonup R^2 pprox 0.83$  (better fit) : NMEA  $\approx 7.94$
- Lower MaxAE and reduced localized losses.

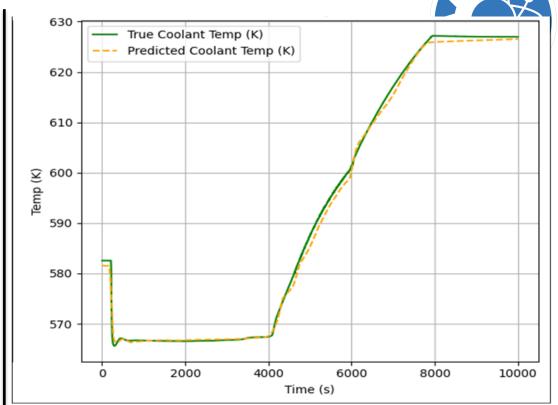


**Coolant Temperature Evolvement** 



**Figure 4: DNN Coolant Temp Trends** 

- Non- Conservative Predictions
- Overshooting

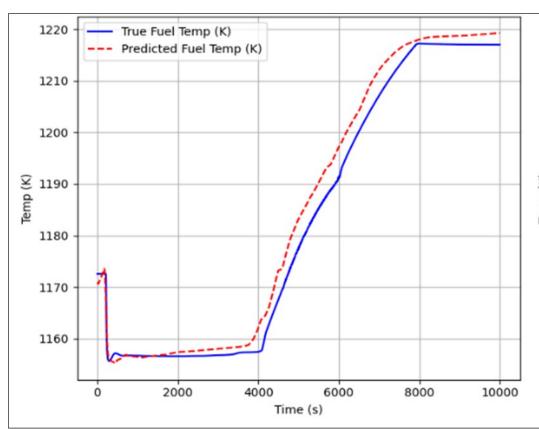


**Figure 5: PINN Coolant Temp Trends** 

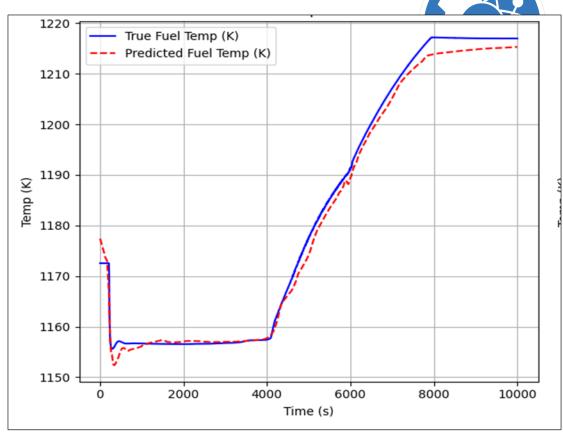
More Stable and Conservative

Statistical fit and physically conservative prediction margin

### **Fuel Temperature Evolvement**



**Figure 6: DNN Fuel Temp Trends** 

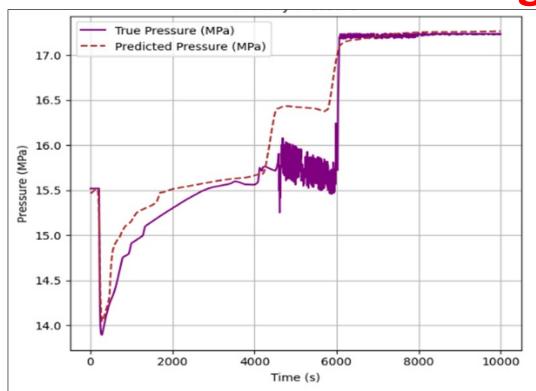


**Figure 7: PINN Fuel Temp Trends** 

Statistical fit and physically conservative prediction margin

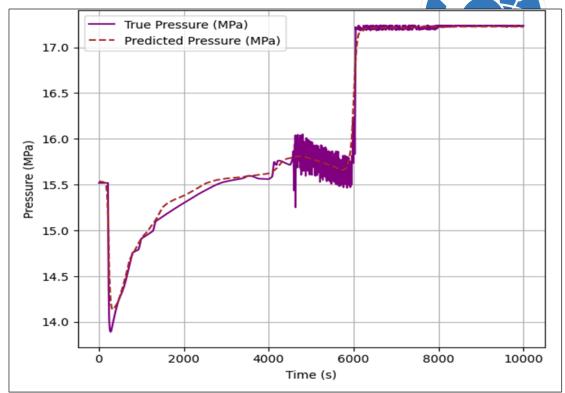


**Pressure Trends During the Accident** 



**Figure 8: DNN Pressure Trends** 

- > Struggling in capturing high oscillations.
- Phase lag relative to true peak



**Figure 9: PINN Pressure Trends** 

- Reducing magnitude of peaks.
- Closely following true data's shape.

Stable physics constrained predictor

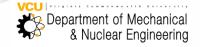
### **Discussion**



# Discussion: Physical Fidelity & Consistency

**Table 4: DNN vs PINN Performance** 

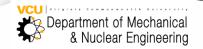
Paramete r	Metri c	Best DNN (TCN)	Best PINN (Shared- Encoder Multi-Head)	Improvement (%)	Comment
$T_f$	RMSE	78.89	52.10	33.9↓	Reduced temp prediction error by one-third.
	MAE	58.94	38.25	35.1↓	Lower average deviation
	$\mathbb{R}^2$	0.76	0.92	+21.1 ↑	Improved physical consistency
$T_C$	RMSE	58.96	41.50	29.6↓	Reduces $T_C$ uncertainty
	MAE	50.54	35.22	30.3 ↓	Improved smoothness and generalization
	$\mathbb{R}^2$	0.16	0.88	+450 ↑	improve prediction
$P_p$	RMSE	0.57	0.39	31.6↓	Reduced prediction uncertainty
	MAE	0.34	0.27	20.6 ↓	Better pressure profile prediction
	$\mathbb{R}^2$	0.74	0.91	+23.0 ↑	Better adherence to system response
Overall	RMS	56.90	44.60	21.6 ↓	Lower deviations across all parameters
Average	$\mathbf{E}$				
	MAE	36.61	27.91	23.8 ↓	Better accuracy and generalization
	R <sup>2</sup>	0.98	0.999	+1.6 ↑	Better consistence between predicted and primary data.



### **Discussion: Physical Fidelity & Consistency**

**Table 5: DNN vs PINN Performance** 

Feature	DNN	PINN
Prediction Stability	Volatility & Spikes (non- physical, high-frequency. It's a statistical curve-fitter)	Physical Smoothness (smoother and more stable)
Safety-Critical Peak Error	Non-Conservative Risk (Frequently exhibits MaxAE)	Conservative Margin (reduces the non- conservative MaxAE risk)
System Coupling	Decoupled (struggles to maintain thermodynamic coupling between variables)	Explicitly Coupled (more consistent system-wide predictions)



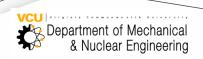
#### **Conclusion & Future Work**

- Both models provided predictions in the millisecond range (necessary for real-time applications.)
- The PINN models achieved 20-30% lower RMSE and 15-25% higher R<sup>2</sup> values across all parameters.
- Future models in reactor control and safety assessment must incorporate physics constraints to satisfy regulatory standards.
- ➤ Efforts to consider developing a higher-fidelity pressure model accounting for two-phase fluid properties.



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#### **Acknowledgments**

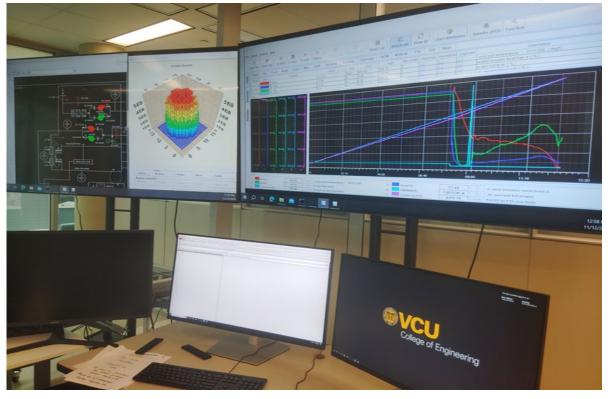




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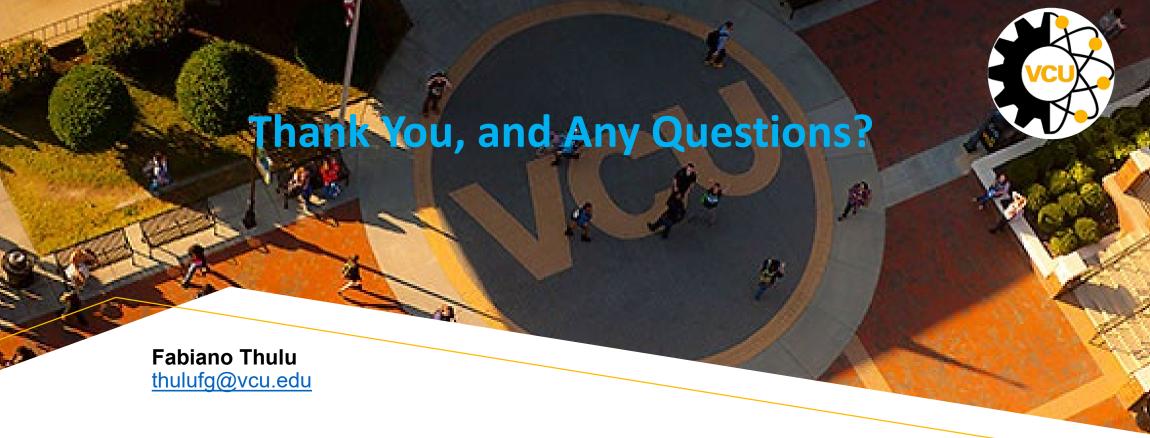
"Improving the computational efficiency and usability of dynamic PRA with reinforcement learning"

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